

Generating 24-Hour ECG, BP and Respiratory Signals with Realistic Linear and Nonlinear Clinical Characteristics Using a Nonlinear Model

GD Clifford¹, PE McSharry^{2,3,4}

¹Harvard-MIT Division of Health Sciences & Technology, Cambridge MA, USA

²Department of Engineering Science, University of Oxford, Oxford, UK

³Mathematical Institute, University of Oxford, Oxford, UK

⁴Centre for the Analysis of Time Series, London School of Economics, London, UK

Abstract

A nonlinear model for generating lifelike human ECG, blood pressure and respiratory signals is described. Each cycle of the model corresponds to one heart beat and the signals therefore exhibit beat-to-beat fluctuations by driving the model with a sequence of RR intervals. By using a modified version of entry no.201 of the CinC 2002 24-hour RR interval generator challenge, (such that the user can specify the probability of ectopy or artefact) and coupling it to three ordinary differential equations, the model generates a 24-hour ECG signal. Using both standard linear metrics, and nonlinear long range statistics, the signal is shown to exhibit many of the known characteristics such as Respiratory Sinus Arrhythmia, Mayer waves and an overall diurnal rhythm.

The RR interval time series is modelled as a set of stationary states (joined by a transient heart rate overshoot) of differing lengths, mean heart rates (HR), LF/HF ratios and standard deviations. The length of time in each state is governed by a power law distribution with marked differences between waking and sleep states. The statistics of each RR time series segment (a state) can be fully specified by its mean (HR) and spectral distribution (LF/HF ratio).

The resultant ECG is shown to exhibit realistic QRS- and QT-dispersions, R-S amplitude modulation and Respiratory Sinus Arrhythmia in the short term and normal values for nonlinear statistics (such as entropy) in the long term. By altering the parameters of the ECG model, introducing a heart-rate dependent delay (to simulate pulse transit time), and coupling the baseline to the long-term fluctuations of the 24 hour RR interval generator, realistic short and long range blood pressure fluctuations are shown to result. Together with seeded RR interval dynamics, the morphology of the signals can be fully specified by three parameters per feature and therefore a large range of different (deterministic) signals can be generated with

fully known characteristics, to facilitate the testing of signal processing algorithms. Open source C, Matlab and Java programs for generating the model are available from *Physionet*.

1. Introduction

In order to effectively test the performance of signal processing algorithms for analysing biomedical signals, a noise-free signal is often desired [1]. A realistic artificial biomedical signal generator that is able to encompass the range of signals observed for both normal and abnormal subjects is therefore a useful tool. Furthermore, the ability to rapidly create a regenerateable time series enables a researcher to quickly prototype applications and test theories such as signal mixing and as a function of the model parameters such as sampling rate [1, 2].

Modifications of our published models for generating artificial 24-hour RR intervals [3] and ECG, blood pressure (BP) and respiration waveforms [1, 2] for generating 24-hour versions of these waveforms are presented. They are shown to have realistic properties; the signal possesses oscillations in morphological features and clinical parameters (such as QRS width, RS amplitude, RR and QT-intervals) as well as statistical similarities with real data on many scales. Furthermore, the signals possess morphological appearances similar to that of a real waveforms and have a realistic inter-signal relationship.

2. Methods

2.1. RR interval sequence

During a 24 hour period, the HR tends to jump between different quantised states, relating to different physical and mental activity [4, 5], with different means \bar{x} , and variances, σ^2 . The 24 hour tachogram is therefore built from a

series of stationary states with prescribed means, variances and LF/HF ratios. See [2] for further explanation. Briefly, the long term oscillations (described in [3]) use empirical power-law distributions found in real data by Bernaola-Galván *et al.* [5]. The length of time τ spent in a given state is governed by a power law distribution with $\tau = (u/\gamma)^{-\rho}$ where $\gamma = 5466.8$, $\rho = 2.2$ and u is the uniform distribution $\sim U(\bar{x}, \sigma)$ with $\bar{x} = 0, \sigma = 1$. Fluctuations due to both a circadian rhythm (including wake-sleep and sleep-wake transitions) and inter-sleep cycles are generated separately.

Circadian activity (high HR during wakefulness and low HR during sleep) leads to an approximately sinusoidal variation in baseline activity throughout the day [4]. During the wake stage, the mean RR interval is $\hat{\mu}_{RR} \sim U(0.7, 1)$, with amplitude $U(0.075, 2.075) \times (\sin[\pi + (2\pi/T_c)t] + \frac{2x}{5})$ and circadian period $T_c \sim N(24, 1)/60^2$ s where r is a zero mean, unit variance normal distribution ($r \sim N(0, 1)$). During the sleep stage, the mean RR interval for a state is $U(0.7, 1) + \frac{1}{2}U(0.1, 0.2) [1 + \sin(2\pi t/T_s)]$ and the period of the sleep cycle is $T_s = 6 \times 10^3$ s. The starting sleep time T_s and sleep duration interval T_d are given by $T_s \sim U(14, 16)/60^2$ s and $T_d \sim U(6, 8)/60^2$ s.

The size of transitions between different mean HRs, $\Delta\mu_{RR}$, are replicated using a distribution with a similar shape to that found from empirical observations [3, 5], $\Delta\mu_{RR} = \frac{1}{2}U(0.03, 0.13)(1 + e^r/10)u/|u|$ with r and u are normal and uniform distributions where $r \sim N(0, 1)$ and $u \sim U(0, 1)$. The length of each transition between states is modelled by $\tau_{trans} \sim U(5, 30)$. The over/undershoot and following compensatory return is replicated by superimposing a V-shaped bridge to span between the first and last RR interval of neighbouring states.

2.2. The ECG & BP and respiratory model

The above RR interval model is then used to drive the angular frequency ψ in the waveform model (described in detail in [1, 2, 6]) which has been modified to accept a vector of RR intervals. Briefly, the ECG is generated by a fourth order Runge-Kutta integration [7] of three ODE's (Ordinary Differential Equations) in a 3D space (x, y, z) . Distinct points on the ECG, such as the P,Q,R,S and T are described by *events* corresponding to negative and positive Gaussian attractors/repellers in the z -direction. These events are placed at fixed angles along the unit circle given by $\theta_P, \theta_Q, \theta_R, \theta_S$ and θ_T which cause the trajectory to deviate from the (x, y) -plane in a Gaussian manner with amplitudes a_i , and widths b_i . The ODE's describing the dynamics are

$$\begin{aligned}\dot{x} &= \psi x - \omega y, \\ \dot{y} &= \psi y + \omega x,\end{aligned}$$

Table 1. ECG & BP model parameters in (1). $\beta = \frac{\sqrt{\text{HR}}}{60}$

Index (i)	P^{ECG}	Q^{ECG}	R^{ECG}	S^{ECG}	T^{ECG}
Time (s)	-0.2	-0.05	0	0.05	0.3
θ_i (rads)	$-\frac{\pi}{3}\beta^{\frac{1}{2}}$	$-\frac{\pi}{12}\beta$	0	$\frac{\pi}{12}\beta$	$\frac{\pi}{2}\beta^{\frac{1}{2}}$
a_i	1.2	-5.0	30.0	-7.5	0.75
b_i	0.25β	0.1β	0.1β	0.1β	0.4β
Index (i)	P^{BP}	Q^{BP}	R^{BP}	S^{BP}	T^{BP}
Time (s)	0.21	0.01	0	0.03	0.22
θ_i (rads)	$-\frac{5\pi}{12}\beta^{\frac{1}{2}}$	$-\frac{\pi}{36}\beta$	0	$\frac{\pi}{18}\beta$	$\frac{4\pi}{9}\beta^{\frac{1}{2}}$
a_i	0	0	0.45	0.25	0.45
b_i	0.25β	0.1β	0.3β	0.5β	0.3β

$$\dot{z} = - \sum_{i \in \{P, Q, R, S, T\}} a_i \Delta\theta_i e^{(-\Delta\theta_i^2/2b_i^2)} - (z - z_0), \quad (1)$$

where $\psi = 1 - \sqrt{x^2 + y^2}$, $\Delta\theta_i = (\theta - \theta_i) \bmod 2\pi$, $\theta = \text{atan2}(y, x)$ and ω is the angular velocity of the trajectory as it moves around the limit cycle. The ECG is the motion of the trajectory in the z -direction. The BP waveform is generated in the same manner, but with different values of θ_i , a_i and b_i (see table 1). The indexes for the BP no longer carry the same interpretation as with the ECG, with $i = R$ corresponding to the first peak and $i = S$ corresponding to the dichrotic notch. Figure 1 illustrates examples of these waveforms and their relationship.

Pulse transmission time (PTT) is therefore $2\pi/(\theta_Q^{BP} - \theta_R^{ECG})$ seconds. PTT is inversely related to the pulse wave velocity down the artery which is known to be influenced by BP, HR, arterial compliance and hence age [8]. The effect of arterial compliance on PTT is not modelled. However, changes in PTT and BP as a function of HR (and therefore RR) interval are incorporated by adding an offset $\delta\theta$ to the θ_i at each beat such that $\delta\theta = (1 - (\frac{60}{\text{HR}}))^{\frac{1}{2}}/2\pi$ to mimic the empirical results of Drinan *et al.* [8]. It is generally accepted that as BP falls, tension in the arterial wall falls and the PTT increases; and vice versa [9]. The systolic (peak) BP has therefore been linearly coupled to the mean HR (and hence inversely to the PTT).

The beat-to-beat variation in the waveform morphologies are induced by the variation in the integration step dt to reflect changes in the RR interval; the time to complete one revolution around the attracting limit cycle in the (x, y) -plane. Shorter RR intervals (higher HR's) compress the waveform, resulting in shorter QT intervals and lower RS amplitudes (i.e. RSA). To mimic Bazett's law, a further compression factor is added; the θ_i are therefore pre-multiplied by a factor proportional to $\beta = \sqrt{\text{HR}}/60$.

The respiratory signal is simply the HF (parasympathetic) oscillation and is generated in the same manner as the RR intervals (using the inverse FT) using only the HF

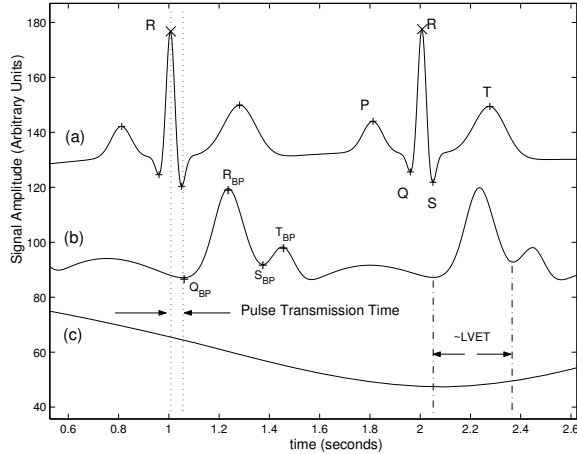


Figure 1. ECG (a), BP (b), and respiratory (c) signals labeled with PTT, LVET and P, Q, R, S, and T points, generated by integrating Eq. (1) over θ_i , a_i and b_i .

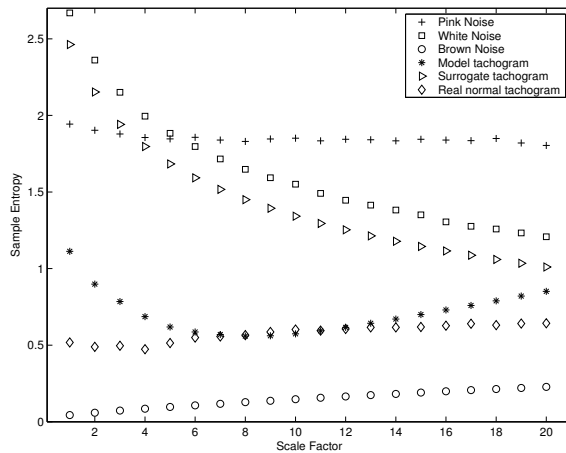


Figure 2. MSE results for model, surrogate, normal, pink noise, white noise and brown noise. See text for details

contribution. If, rather than being internally generated, the RR interval sequence is supplied as a vector, then the HF component of the signal is extracted by band pass filtering the signal between 0.1 and 0.5 Hz. The sequence is then resampled to the desired output frequency.

3. Results

Linear metric results such as Realistic values for beat-to-beat and HR-related amplitude modulation, QRS-width and QT-dispersion, and PR interval changes have already been reported for this model [2]. Since the BP signal is generated in the same manner as the ECG, the dynamics that affect the ECG also affect the BP signal. These have also been noted in a previous publication [1]. In particular

we ensure that the random addition to the PTT results in a correlation ρ between the PTT and RR interval that is no less than 0.7 as per Drinnan *et al.* [8]. The left ventricular ejection time (LVET) is proportional to the time between the onset of the BP waveform and the start of the reflected wave (the points θ_Q^{BP} and θ_S^{BP} in figure 1). The LVET has been shown to be longer for lower HR [10], a relationship that naturally emerges from the model presented here.

Although many nonlinear statistics have been applied to the ECG and BP waveforms, no clear consensus on the applicability of these metrics to the description of these waveforms has emerged [11]. We therefore confine our nonlinear analysis to the beat-to-beat interval dynamics. Detrended Fluctuation Analysis (DFA)[12] was employed in order to determine the long range correlations in the data. For one hundred random seeds, we found a pink noise-like scaling exponent of $\alpha = 1.02 \pm 0.01$, which is in agreement for the α 's reported for healthy subjects [12]. Position randomised surrogates of these tachograms gave $\alpha = 0.50 \pm 0.01$, a white noise scaling behaviour. The *cross-over* phenomenon at $\log_{10}(n) \approx 1.5$ is also observed.

A further complimentary scaling behaviour metric known as Multi Scale Entropy (MSE) [13] was also employed and compared to surrogates, real data, pink, white and brown noise (see figure 2). The scaling of the data was often patient specific (probably due to age differences [13]). For subject 040 of the NSRDB (illustrated in figure 2) the scaling behaviour is between pink and brown noise. This is consistent with the DFA scaling found for the same subject. The model scaling is consistent with the real data, particularly at the central scales. Similar results were found for BP intervals, with PTT having little effect on the scaling.

4. Discussion

Slight departures from normal behaviour of the MSE scaling for the model at extreme scales indicates that improvements could be made in the very short-term and very long-term behaviour of the model. In particular, the movement of the scaling towards pink and white noise behaviours for high (short) scales indicates that there is need for a more it Brownian-like complexity with a greater correlation between beat-to-beat intervals. This indicates that although the Fourier-inversion process to create the short sections of RR intervals produces a series of spectra with realistic LF/HF values, the time-correlations of the data are not realistic enough. Although one may replace the short term RR interval creation process with a more realistic, physiology-based model (such as IPFM [14] or CVSIM [15]), it is not clear how the 24-hour distributions of RR interval model can be preserved.

A possible explanation for the MSE disparity at longer

scales is the lack of intrinsic correlation between mean HR and LF/HF ratios from segment to segment. In particular, during sleep, a subject will oscillate between deep and lighter sleep with slowly shortening and lengthening periods, which are often well correlated with shifts in the LF/HF ratio and mean heart rates. This structure is not entirely mimicked in this model and only an overall shift in all the system parameters is seen. Furthermore, no explicit arousal mechanism exists in the model.

Although the ECG and BP signals exhibit a natural morphology (and changes) which can be adapted to any given patient, the respiratory signal lacks realism since it is too periodic. To introduce a more realistic morphology into the latter signal and mimic the asymmetry between exhalation and inhalation, it may prove useful to skew the signal in a manner proportional to the positive gradient. It should also be noted that no explicit delays have been built into the system to account for the pre-ejection period (PEP) and the ejection time (ET). However, a user-definable PTT relationship has been incorporated, and therefore the PEP and ET can be factored into this relationship if required.

5. Conclusions

The model presented in this paper comprises of two separate models; one for the beat-to-beat timing interval process and one for generating waveforms (such as the ECG, BP or respiratory signal) from these RR intervals. Model parameters are initialised using realistic distributions that can be modified so that different seeds produce different but repeatable biomedical signals. While the overall model is relatively complex, it summarises many of the important physiological control mechanisms that influence HR, BP and respiration over 24 hours and their short term inter-signal relationships. Since each of the parameters of each model has a very clear physiological meaning, the performance of signal processing algorithms (such as how they respond to specific changes or contaminants) can be tested on a variety of artificial biomedical time series and may aid the teaching of the underlying mechanisms. Open source C, Matlab and Java code for these models is available from Physionet [6].

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Address for correspondence:

Gari D. Clifford
 Laboratory for Computational Physiology
 Harvard-MIT Division of Health Sciences & Technology
 Rm E25-505, 45 Carleton St.,
 Cambridge MA 02142 USA
 gari@mit.edu